

single-threaded-relation3^{11,40}

$\forall es:\text{ES}, P:(\text{E} \rightarrow \mathbb{P}), R:(\text{E} \rightarrow \text{E} \rightarrow \mathbb{P}).$
 $(\forall e:\text{E}. \text{Dec}(P(e)))$
 $\Rightarrow (\forall e, e':\text{E}. \text{Dec}(R(e',e)))$
 $\Rightarrow R = \lambda x,y. (x < y)$
 $\Rightarrow (\forall e, e':\text{E}. (P(e) \& R(e',e)) \Rightarrow P(e'))$
 $\Rightarrow (\forall m, m':\text{E}.$
 $P(m) \Rightarrow P(m') \Rightarrow (\forall e:\text{E}. (e R m) \Rightarrow (\neg P(e))) \Rightarrow (\forall e:\text{E}. (e R m') \Rightarrow (\neg P(e))) \Rightarrow (m = m'))$
 $\Rightarrow (\forall a, b, e:\text{E}.$
 $(\forall x, y:\text{E}. x \leq e \Rightarrow y \leq e \Rightarrow P(x) \Rightarrow P(y) \Rightarrow (((x R^+ y) \vee (x = y)) \vee (y R^+ x)))$
 $\Rightarrow (R(e,a) \& R(e,b))$
 $\Rightarrow (P(e) \& P(a) \& P(b))$
 $\Rightarrow (\forall z:\text{E}. \neg(R^+(e,z) \& R^+(z,a) \& P(z)))$
 $\Rightarrow (\forall z:\text{E}. \neg(R^+(e,z) \& R^+(z,b) \& P(z)))$
 $\Rightarrow (a = b))$
 $\Rightarrow (\forall e, e':\text{E}. P(e) \Rightarrow P(e') \Rightarrow (((e R^+ e') \vee (e = e')) \vee (e' R^+ e)))$